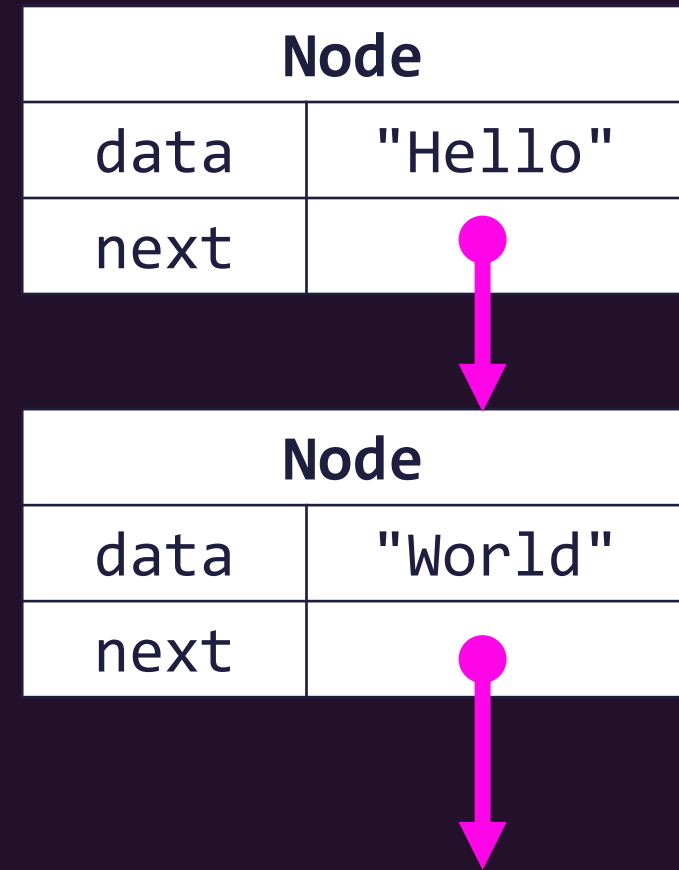


Recursive Data Structures !

Recursive Data Types

- An attribute *can* refer to another object of the *same type*
- Notice the class `Node`. The attribute named `next` is... *another Node!*
- This is a recursive data type!
- We'll discuss how to initialize a recursive property to avoid infinite recursion shortly...

```
class Node:  
    data: int  
    next: Node
```



Data Structures

- You can use this ability to form **data structures** with different properties and uses.
- In COMP110, you'll explore the Singly-linked List (left)
- In COMP210, you'll explore other data structures like Trees (right) and Graphs

```
class Node:
```

```
    data: int
```

```
    next: Node
```

Node	
data	1
next	●



Node	
data	2
next	●



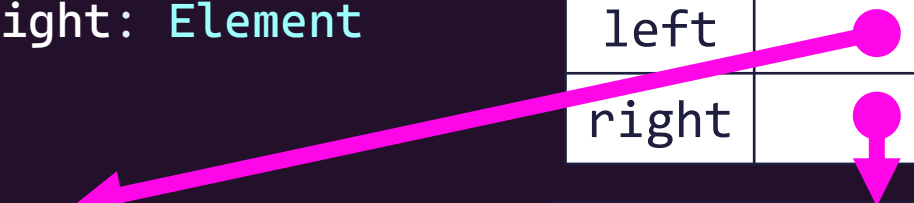
```
class Element:
```

```
    data: int
```

```
    left: Element
```

```
    right: Element
```

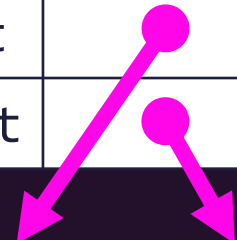
Element	
data	2
left	●
right	●



Element	
data	1
left	●
right	●



Element	
data	3
left	●
right	●



Linked List

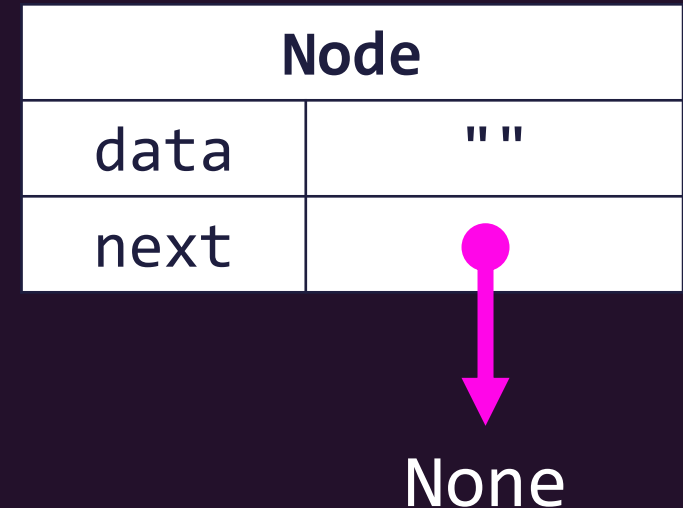
- A classic, simple data structure in Computer Science
- Formed by chaining together a sequence of objects
 - The first node is conventionally called the **head**
 - Our focus is on singly-linked lists, meaning a Node only references the Node after it
- Linked Lists are more cumbersome to work with than Python's List
 - However, they're *amazing* for understanding and exploring fundamentals including:
 - **None** / "null" values
 - References
 - Recursive algorithms



What is a recursive attribute's "base case"?

- If a Node refers to a next Node, and the next Node refers to another next Node, then *when does it end?*
- Recursive attributes are **terminated** with a **None** value.
 - In *many* other languages this is called **Null**.
 - It is a "reference to nowhere" that you can read as "this attribute refers to nothing."
 - For static typing purposes, we declare `Optional[RecursiveType]`
- Our linked lists is "**None terminated**" or, commonly, "Null terminated"

```
class Node:  
    data: int  
    next: Optional[Node]
```



What are the fundamental operations of a singly Linked List?

1. You can *construct* a new Node at the front of another linked list
 - via the *Node* constructor
 2. You can access a linked list's first value
 - via the *data* attribute
 3. You can access the rest of the list, excluding the first Node
 - via the *next* attribute
- That's it! These are the fundamental *capabilities* we need.
 - Using these simple operations, you will write more advanced functions, or abstractions, to perform more sophisticated tasks with linked lists.
 - Notice we are intentionally deciding to treat a constructed Node as immutable, we are not going to modify its data or next attributes after construction.

The count Algorithm: Counting Nodes in a Linked List

- How can we write a function that, given a List of any length, we can count the number of elements in it?
- Let's try it with *pseudo-code* first!
- **Count Algorithm, Given any List**
 1. *If* the List is empty, *then* the count is 0
 2. *Else*, count is 1 + the count algorithm applied to *the rest of* the List

Rules of Recursive Algorithms

When processing a recursive data structure recursively:

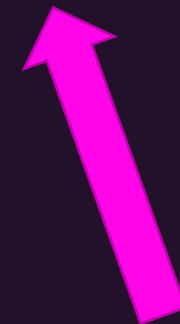
1. Always test to see if the structure is *empty* (equal to None)
 - This is a **base case**!
2. Make the recursive call on a subpart of the structure
 - With a singly linked list, this is always going to be the *next* Node.

Rules of Recursion using Linked Lists

1. Always check if list is empty! This is the base case.



```
def count(head: Optional[Node]) -> int:  
    if head is None:  
        return 0  
    else:  
        after_me = count(head.next)  
        return after_me + 1
```



2. Make the recursive call with the *rest of the list*.

Recursive Diagramming

```
1  from __future__ import annotations
2  from typing import Optional
3
4  class Node:
5      data: int
6      next: Optional[Node]
7
8      def __init__(self, data: int, next: Optional[Node]):
9          self.data = data
10         self.next = next
11
12
13  def count(head: Optional[Node]) -> int:
14      if head is None:
15          return 0
16      else:
17          after_me = count(head.next)
18          return after_me + 1
19
20
21  n0 = Node(21, None)
22  n1 = Node(18, n0)
23  print(count(n1))
```

Does a Linked List *include* a specific value?

True/False

- How can we write a function that, given a list list of any length and a search value, we can check to see if the list contains that value?
- Let's try it with *pseudo-code* first!
- **Includes Algorithm**, Given any list and a value **V**
 1. If the List is empty, then the List does not include V, return false!
 2. Else,
 1. If the first value in the List equals **V**, return true!
 2. Else, run the includes algorithm on the rest of the list

Follow-along: Implementing includes in Code

- Let's implement the includes function together!

Rules of Recursion using Linked Lists

```
def includes(head: Optional[Node], needle: int) -> bool:
    if head is None:
        return False
    elif head.data == needle:
        return True
    else:
        return includes(head.next, needle)
```